1. Briefly describe the following questions.
(a) Please use cascode and ratio matching techniques to design a wide-swing current mirror, as shown in Fig. P1(a), which can generate accurate $0.6 \times \mathrm{I}$. Describe your design and draw your schematic. Do not apply any DC voltages except $V_{D D}$ and GND.
(b) Explain pole-zero frequency doublet with the first stage of a two-stage OPAMP shown in Fig. P1(b) by showing that $\frac{i_{\text {out }}}{v_{\text {in }}}=g_{m 1} \cdot\left(\frac{1+s / 2 \omega_{p}}{1+s / \omega_{p}}\right)$, where $\omega_{p}=\frac{g_{m 3}}{C_{x}}$. Assume $g_{m 1}=g_{m 2}, g_{m 3}=g_{m 4}, C_{x}=C_{g s 3}+C_{g s 4}$ $+\mathrm{C}_{\mathrm{db} 1}+\mathrm{C}_{\mathrm{db} 3}+\mathrm{C}_{\mathrm{gd} 1}$.
(c) Briefly describe mobility degradation.
(d) Describe flicker noise and how to reduce it. Explain the correlated double sampling (CDS) circuit.
(e) Briefly describe noise bandwidth and how $\mathrm{kT} / \mathrm{C}$ noise is generated.
(f) Briefly explain how to prevent latch-up problem.
(g) Briefly describe device mismatch and list two major capacitor mismatch errors. How to get accurate resistor and capacitor ratios?
(h) Briefly explain yield and what factors affect it.
(i) Briefly explain antenna rule.
(j) Briefly describe subthreshold operation of MOSFET.
(k) Briefly describe how to set the input and output common mode voltage of single-ended and fullydifferential ended resistive-feedback inverting amplifier with its closed loop gain $=-R_{1} / R_{2}$, respectively.
(1) What is the full power bandwidth of an OPAMP with a rated output voltage of 1 V and a slew rate of $1 \mathrm{~V} / \mathrm{ns}$ ?
(m)Describe the purpose of capacitor layout with equal perimeter-to-area ratio, and show a capacitor layout with equal perimeter-to-area ratios of 2 units and 3.35 units, where a unit-sized capacitor is $10 \mu \mathrm{mx}$ $10 \mu \mathrm{~m}$. (Hint: when a non-unit-size is required, it is usually set to between one and two times the unitsized capacitor and is rectangular in shape, ex : 3.35units=2units +1.35 units.)
(n) Briefly describe how to design a high gain and wideband amplifier with accurate gain and bandwidth. (Hint: feedback, multi stage and switching capacitor may be used to realize such requirement)


Fig. P1(a)


Fig. P1(b)
2. Two voltage amplifiers (each having infinite input impedance and zero output impedance) are available: one with a gain of $3 \mathrm{~V} / \mathrm{V}$ and $6 \mu \mathrm{~V}_{\text {rms }}$ noise observed at the output; the other with a gain of $10 \mathrm{~V} / \mathrm{V}$ and $15 \mu \mathrm{~V}_{\mathrm{rms}}$ noise observed at its output.
(a) What is the input-referred noise of each amplifier?
(b) If the two amplifiers are to be placed in series to realize a gain of $30 \mathrm{~V} / \mathrm{V}$, in what order should they be placed to obtain the best noise performance?
(c) What is the resulting input-referred noise of the overall system in (b)?
3. Answer the following questions.
(a) Find the total rms noise value if three uncorrelated noise sources having $\mathrm{V}_{\mathrm{n} 1 \_\mathrm{rms}}=7 \mu \mathrm{~V}, \mathrm{~V}_{\mathrm{n} 2} \mathrm{rms}=3 \mu \mathrm{~V}$ and $V_{n 3 \_r m s}=4 \mu \mathrm{~V}$ are combined.
(b) Consider an ideal noiseless amplifier with voltage gain of 40 dB , and the load capacitor $\mathrm{C}_{\mathrm{L}}$, in parallel with a load resistor, $\mathrm{R}_{\mathrm{L}}$, as shown in Fig. P3, where $\mathrm{V}_{\mathrm{RL}}(\mathrm{f})$ is the thermal noise of $\mathrm{R}_{\mathrm{L}}$. Assuming $\mathrm{T}=300 \mathrm{~K}, \mathrm{C}=3 \mathrm{pF}, \mathrm{R}=150 \mathrm{k} \Omega$, and $\mathrm{k}=1.38 \times 10^{-23} \mathrm{JK}^{-1}$, please calculate the squared rms noise across the capacitor, $\mathrm{V}_{\text {no_rms }}{ }^{2}$ and the squared rms input-referred noise of the circuit.


Fig. P3
4. Fig. P4(a) shows a comparator using an OPAMP, where $\Phi_{1}, \Phi_{1 \mathrm{a}}$, and $\Phi_{2}$ is shown in Fig. P4(b) and the OPAMP is assumed to be ideal. Describe the operation of offset cancellation in Fig. P4(a).


Fig. P4(a)
5. As shown in Fig. P5, there is a cascaded n-stage comparator. Derive the gain $\mathrm{A}_{\mathrm{c}}$ of each stage to get the minimum total time constant $\left(\tau_{\text {total }}=\Sigma \tau \mathrm{i}\right.$, where $\left.\tau \mathrm{i}=1 / \omega_{3 \mathrm{~dB}}\right)$, assuming the total gain $\left(\mathrm{A}_{\text {tot }}\right)$ of the comparator is a constant and corner frequency $\omega_{3 \mathrm{~dB}}$ of each stage is the same. Hint : $\partial A^{n} / \partial n^{n}=A^{n} \cdot \ln (A)$



Fig. P5
6. Show the frequency response of $\mathrm{V}_{\text {out }}(\mathrm{s}) / \mathrm{V}_{\mathrm{DD}}(\mathrm{s})$ in Fig.P6, with the parameters of $\mathrm{C}_{\mathrm{gs}}, \mathrm{g}_{\mathrm{m}}, \mathrm{r}_{\mathrm{ds}}$ and $\mathrm{C}_{\mathrm{L}}$. In addition, $\mathrm{C}_{\mathrm{gd}}, \mathrm{C}_{\mathrm{gb}}, \mathrm{C}_{\mathrm{sb}}$, and $\mathrm{C}_{\mathrm{db}}$ of MOSFETs can be neglected.


Fig. P6
7. A constant $g_{m}$ bias circuit is shown in Fig. P7(a). Neglect channel length modulation and body effect.
(a) For Fig. P7a, please find $\mathrm{I}_{\text {REF }}$ (non-zero solution) in terms of $\mu_{\mathrm{p}} \mathrm{C}_{\mathrm{ox}}, ~(\mathrm{~W} / \mathrm{L})_{\mathrm{p}}, ~ \mathrm{R}$ and $\mathrm{K}(\mathrm{K}>1)$.
(b) According to the circuit shown in Fig. P7(b), find the DC loop gain, $\mathrm{A}_{0}=\left(\mathrm{V}_{\mathrm{o}} / \mathrm{V}_{\mathrm{i}}\right)$ in $\mathrm{g}_{\mathrm{m} 1}, \mathrm{~g}_{\mathrm{m} 2}$ and R .
(c) Let $\mathrm{K}=4$, what is the value of DC loop gain $\mathrm{A}_{0}$ ?


Fig. P7(a)


Fig. P7(b)
8. For a single-stage fully differential OPAMP and its common-mode feedback (CMFB) block diagram shown in Fig. P8, where $\mathrm{V}_{\text {BIAS_P }}, \mathrm{V}_{\mathrm{BN}}$ and $\mathrm{V}_{\mathrm{CM}}$ are DC voltage, the transistor sizes are given in Table P8. Assume $\mu_{\mathrm{n}} \mathrm{Cox}_{\mathrm{ox}}=100 \mu \mathrm{~A} / \mathrm{V}^{2}, \mu_{\mathrm{P}} \mathrm{C}_{\mathrm{ox}}=40 \mu \mathrm{~A} / \mathrm{V}^{2}, \mathrm{~V}_{\mathrm{tn}}=-\mathrm{V}_{\mathrm{tp}}=0.5 \mathrm{~V}, \mathrm{~V}_{\mathrm{DD}}=1.8 \mathrm{~V}, \lambda_{\mathrm{n}}=\lambda_{\mathrm{p}}=0.05 / \mathrm{L}(\mu \mathrm{m})$, $\mathrm{I}_{\mathrm{D} \_\mathrm{M} 1}=\mathrm{I}_{\mathrm{D} \_\mathrm{M} 2}=10 \mu \mathrm{~A}, \mathrm{a}_{\mathrm{cms}}=1$ and body effect can be neglected.
(a) Briefly describe the operational principle of CMFB block diagram shown in Fig. P8. (5\%)
(b) Calculate the DC gain of common-mode loop gain. (10\%)
(Hint: common-mode loop gain $=\frac{\mathrm{V}_{\mathrm{ctr}}(\mathrm{s})}{\mathrm{V}_{\mathrm{oc}}(\mathrm{s})} \cdot \frac{\mathrm{V}_{\mathrm{o}}^{+}(\mathrm{s})}{\mathrm{V}_{\mathrm{ctr}}(\mathrm{s})}$ or $\left.\frac{\mathrm{V}_{\mathrm{ctr}}(\mathrm{s})}{\mathrm{V}_{\mathrm{oc}}(\mathrm{s})} \cdot \frac{\mathrm{V}_{\mathrm{o}}^{-}(\mathrm{s})}{\mathrm{V}_{\mathrm{ctr}}(\mathrm{s})}\right)$


Table P8
The dimension of
transistors (in $\mu \mathrm{m}$ )

| M1 | $32 / 1$ |
| :--- | :--- |
| M2 | $32 / 1$ |
| M3 | $12 / 1$ |
| M4 | $12 / 1$ |
| M5 | $64 / 1$ |

Fig. P8
9. Fig. P9 shows enhanced output-impedance current mirror, where the current source is ideal and the transistor sizes are in Table P9. Assume $\mu_{\mathrm{n}} \mathrm{Cox}=100 \mu \mathrm{~A} / \mathrm{V}^{2}, \mu_{\mathrm{p}} \mathrm{Cox}=40 \mu \mathrm{~A} / \mathrm{V}^{2}, \mathrm{~V}_{\mathrm{tn}}=-\mathrm{V}_{\mathrm{tp}}=0.5 \mathrm{~V}$, $\mathrm{V}_{\mathrm{DD}}=1.8 \mathrm{~V}, \lambda_{\mathrm{n}}=\lambda_{\mathrm{p}}=0.05 / \mathrm{L}(\mu \mathrm{m})$. Neglect $\lambda$ and body effect when determining DC voltage and current.
(a) Show that the output impedance $\mathrm{R}_{\mathrm{O}}$ in Fig. P9 can be approximated as $(1+\mathrm{A}) \mathrm{g}_{\mathrm{m} 1} \mathrm{r}_{\mathrm{ds} 1} \mathrm{r}_{\mathrm{d} \mathrm{s} 2}$.
(b) Assuming A=50, calculate the output impedance in Fig. P9.


Fig. P9
10. For a two-stage OPAMP and a bias circuit shown in Fig. P10, where $\mathrm{C}_{\mathrm{C}}=0.2 \mathrm{pF}, \mathrm{C}_{\mathrm{L}}=2 \mathrm{pF}$ and input bias voltage $=0.8 \mathrm{~V}$, the transistor sizes are given in Table P10. Assume $\mathrm{V}_{\mathrm{DD}}=1.8 \mathrm{~V}, \mu_{\mathrm{n}} \mathrm{Cox}=200 \mu \mathrm{~A} / \mathrm{V}^{2}$, $\mu_{\mathrm{p}} \mathrm{Cox}=80 \mu \mathrm{~A} / \mathrm{V}^{2}, \mathrm{~V}_{\mathrm{tn}}=-\mathrm{V}_{\mathrm{tp}}=0.5 \mathrm{~V}, \lambda=\lambda_{\mathrm{n}}=-\lambda_{\mathrm{p}}=0.06 / \mathrm{L}(\mu \mathrm{m})$, neglect $\lambda$ effect and mismatch errors when determining DC voltage and current.
(a) Calculate DC currents of $\mathrm{I}_{1}$ and $\mathrm{I}_{2}$
(b) Calculate DC voltages of $\mathrm{V}_{1}, \mathrm{~V}_{2}$ and $\mathrm{V}_{3}$.
(c) Calculate the input common mode range of the OPAMP.
(d) Calculate the DC gain of the OPAMP.
(e) Assuming the parasitic capacitance of all transistors can be neglected. To place the right-half-place zero on the $2^{\text {nd }}$ pole, calculate the W of Mc . (Hint: the right-half-place zero is at

$$
\left.\omega_{\mathrm{z}}=\frac{-1}{\mathrm{C}_{\mathrm{c}}\left(1 / \mathrm{g}_{\mathrm{m} 7}-\mathrm{R}_{\mathrm{C}}\right)}\right)
$$

(f) Assuming the W and threshold voltage of M 1 become $5.2 \mu \mathrm{~m}$ and 0.45 V respectively due to process variation, calculate the input offset voltage. (5\%) (Hint: Input offset voltage is the voltage applied to the input to drive the small signal output voltage to zero)


Table P10

| The dimension of transistors $($ in $\mu \mathrm{m})$ |  |  |  |
| :--- | :--- | :--- | :--- |
| M1 | $5.0 / 0.5$ | M1 | $7.5 / 0.5$ |
| M2 | $5.0 / 0.5$ | Mb1 | $2.0 / 0.5$ |
| M3 | $2.0 / 0.5$ | Mb2 | $2.0 / 0.5$ |
| M4 | $2.0 / 0.5$ | Mb3 | $1.5 / 0.5$ |
| M5 | $12 / 0.5$ | Mb4 | $1.5 / 0.5$ |
| M6 | $15 / 0.5$ | Mc | $\mathrm{W}_{0} 0.5$ |

Fig. P10
11. Two structures of high output impedance current mirrors are shown in Fig.P11, where the current sources are ideal and the transistor sizes are shown in Table P11. Assume $V_{D D}=1.8 \mathrm{~V}, \mu_{\mathrm{n}} \mathrm{Cox}_{\mathrm{ox}}=200 \mu \mathrm{~A} / \mathrm{V}^{2}$, $\mu_{\mathrm{p}} \mathrm{C}_{\mathrm{ox}}=80 \mu \mathrm{~A} / \mathrm{V}^{2}, \mathrm{~V}_{\mathrm{tn}}=-\mathrm{V}_{\mathrm{tp}}=0.4 \mathrm{~V}, \lambda=\lambda_{\mathrm{n}}=-\lambda_{\mathrm{p}}=0.2 / \mathrm{L}(\mu \mathrm{m})$. Neglect $\lambda$ when calculating DC voltage and current.
(a) Please calculate output impedance $\mathrm{R}_{\mathrm{OI}}$ and minimum output voltage $\mathrm{v}_{\mathrm{OI}}$ in Fig. P11(a).
(b) Please calculate output impedance $\mathrm{R}_{\mathrm{O} 2}$ and minimum output voltage $\mathrm{v}_{\mathrm{O} 2}$ in Fig. P11(b).
(c) Please modify the circuit in Fig.P11(a) into a wide-swing cascode structure. Simply sketch your answer (use additional bias circuit if needed) and recalculate the minimum output voltage vor.
(d) If $(\mathrm{W} / \mathrm{L})_{\mathrm{M} 8}$ becomes $6.3 / 0.5$ and $(\mathrm{W} / \mathrm{L})_{\mathrm{M} 7}$ becomes $5.7 / 0.5$, please calculate minimum $\mathrm{v}_{\mathrm{o}}$.


Fig. P11(a)


Fig. P11(b)

Table P11
Transistor dimension

| (in $\mu \mathrm{m}$ ) |  |  |  |
| :---: | :---: | :---: | :---: |
| $\mathrm{M}_{1}$ | $5 / 0.5$ | $\mathrm{M}_{5}$ | $3 / 0.5$ |
| $\mathrm{M}_{2}$ | $5 / 0.5$ | $\mathrm{M}_{6}$ | $9 / 0.5$ |
| $\mathrm{M}_{3}$ | $6 / 0.5$ | $\mathrm{M}_{7}$ | $6 / 0.5$ |
| $\mathrm{M}_{4}$ | $6 / 0.5$ | $\mathrm{M}_{8}$ | $6 / 0.5$ |

12. Fig. P12(a) shows a comparator composed of a pre-amplifier and a positive-feedback latch. The waveforms of the internal nodes are illustrated in Fig. P12(b). Assume the preamplifier output can be expressed as $\mathrm{v}_{\mathrm{p}}(\mathrm{t})=\mathrm{A}_{\mathrm{pre}} \times \Delta \mathrm{V}_{\text {in }}\left[1-\exp \left(-\mathrm{t} / \tau_{\mathrm{pre}}\right)\right]+\mathrm{V}_{\mathrm{DD}} / 2$, where $\mathrm{V}_{\mathrm{DD}} / 2$ is the common-mode voltage of the pre-amplifier, and the two inverters are identical.
(a) If $v_{0}(t)=v_{X}(t)-v_{Y}(t)$, and $v_{o}\left(t_{1}\right)=\Delta V_{O}$. Please refer to Fig.P12(b) and prove that $v_{o}(t)=\Delta V_{o} \times \exp \left(\frac{t-t_{1}}{R_{L} C_{L} /\left(A_{\text {inv }}-1\right)}\right)$ for $t_{1}<t<t_{1}+t_{2}$, where $A_{\text {inv }}, C_{L}$ and $R_{L}$ are the inverter gain, total capacitance of each node $v_{X}$ and $v_{Y}$, and total resistance of each node $v_{X}$ and $v_{Y}$, respectively.
(b) Please refer to Fig. P12(b) and find the time interval $\mathrm{t}_{2}$, which is the time it takes for vo to reach 1.7 V after $\mathrm{t}_{1}$, where $\mathrm{VDD}=1.8 \mathrm{~V}, \mathrm{t}_{1}=50 \mathrm{ps}, \Delta \mathrm{V}_{\text {IN }}=0.7 \mu \mathrm{~V}, \tau_{\text {pre }}=2 \mathrm{~ns}, \mathrm{R}_{\mathrm{L}}=10 \mathrm{k} \Omega, \mathrm{C}_{\mathrm{L}}=0.5 \mathrm{pF}, \mathrm{A}_{\text {inv }}=181$ and the preamp gain $\mathrm{A}_{\mathrm{pre}}=120$. Assume the driving capability of PMOS and NMOS of the inverter are the same and $\mathrm{v}_{\mathrm{o}}\left(\mathrm{t}_{1}\right)=\mathrm{v}_{\mathrm{p}}\left(\mathrm{t}_{1}\right)$.


Fig. P12(a)
13. A comparator design usually employs preamplifier with offset cancellation and a positive feedback latch as shown in Fig. P13(a). The internal nodal voltage waveforms of this comparator are shown in Fig. P13(b). Specifically, the gain and output time constant of this preamplifier are A and $\tau$, respectively. The clock period of this comparator is $T$. The output of the preamplifier can be expressed as $\mathrm{V}_{\text {preamp }}(\mathrm{t})=\mathrm{V}_{\mathrm{DD}} / 2+\mathrm{A}^{*} \mathrm{~V}_{\text {in }}\{1-\exp [-(\mathrm{t}-\mathrm{nT}) / \tau]\}$ for $\mathrm{t} \in\left[\mathrm{nT}, \mathrm{nT}+\mathrm{T}_{1}\right]$ if the offset voltage $\left(\mathrm{V}_{\text {off }}\right)$ of the preamplifier are zero. (Assume all switches are ideal).
(a) Considering finite $A$, please modify the equation of $V_{\text {preamp }}(t)$ for $t \in\left[n T, n T+T_{1}\right]$ if $V_{\text {off }}$ is non-zero.
(b) If the differential output $\mathrm{V}_{\mathrm{o}}(\mathrm{t})=\mathrm{V}_{\mathrm{x}}(\mathrm{t})-\mathrm{V}_{\mathrm{y}}(\mathrm{t})$, and $\Delta \mathrm{V}_{\mathrm{o}}=\mathrm{V}_{\text {preamp }}\left(\mathrm{n} T+\mathrm{T}_{1}\right)-\mathrm{V}_{\mathrm{DD}} / 2$. Please prove ,

$$
V_{o}(t)=\Delta V_{o} \times \exp \left[\frac{t-n T-T_{1}}{\left(R_{L} C_{L} /\left(A_{\text {inv }}-1\right)\right.}\right] \text { for } t \in\left[n T+T_{1},(n+1) T\right]
$$

where $A_{\text {inv }}, C_{L}$ and $R_{L}$ are the inverter gain, total capacitance of each node $V_{x}$ and $V_{y}$, and total resistance of each node $V_{x}$ and $V_{y}$, respectively. Assume the two inverters are identical.
(c) Let $\tau=4 \mathrm{~ns}, \mathrm{~T}_{1}=1 \mathrm{~ns}, \mathrm{R}_{\mathrm{L}}=5 \mathrm{k} \Omega, \mathrm{C}_{\mathrm{L}}=1 \mathrm{pF}, \mathrm{A}_{\text {inv }}=51, \mathrm{~A}=80, \mathrm{~V}_{\text {off }}=1 \mathrm{mV}$ and $\mathrm{V}_{\text {in }}=1.5 \mathrm{mV}$. What is the minimum value of period T for this comparator to let $\left|\mathrm{V}_{\mathrm{o}}(\mathrm{t})\right| \geqq 0.9 \mathrm{~V}_{\mathrm{DD}}$ for $\mathrm{t} \in\left[\mathrm{nT}+\mathrm{T}_{1},(\mathrm{n}+1) \mathrm{T}\right]$ ?
(d) Digital circuit at the comparator differential output requires $-0.9 \mathrm{~V}_{\mathrm{DD}}$ and $0.9 \mathrm{~V}_{\mathrm{DD}}$ for valid logic " 0 " and " 1 ", respectively. With parameters in (c), if $T=2 n s$, find the range of $V_{\text {in }}$ causing metastability.


Fig. P13(a)

14. An OPAMP is shown as Fig.P14, where $\mathrm{C}_{\mathrm{c}}=0.5 \mathrm{pF}, \mathrm{C}_{\mathrm{L}}=2 \mathrm{pF}$ and input bias voltage $=0.9 \mathrm{~V}$. Assume $\mathrm{V}_{\mathrm{DD}}=1.8 \mathrm{~V}, \mu_{\mathrm{n}} \mathrm{C}_{\mathrm{ox}}=200 \mu \mathrm{~A} / \mathrm{V}^{2}, \mu_{\mathrm{p}} \mathrm{C}_{\mathrm{ox}}=80 \mu \mathrm{~A} / \mathrm{V}^{2}, \mathrm{~V}_{\mathrm{tn}}=-\mathrm{V}_{\mathrm{tp}}=0.4 \mathrm{~V}, \lambda=\lambda_{\mathrm{n}}=-\lambda_{\mathrm{p}}=0.2 / \mathrm{L}(\mu \mathrm{m})$. Neglect $\lambda$ and mismatch error when calculating DC voltage and current.
(a) Calculate $\mathrm{I}_{2}, \mathrm{~V}_{1}, \mathrm{~V}_{2}$, and $\mathrm{V}_{3}$.
(b) To eliminate the right-half-place zero altogether $\left(\omega_{z} \rightarrow \infty\right)$, calculate the W of $\mathrm{M}_{\mathrm{c}}$.
(c) For the condition in (b), calculate the DC gain, unity-gain frequency and phase margin.
(d) Please calculate the value of rising slew rate shown in Fig.P14.


Table P14
Transistor dimension

| (in $\mu \mathrm{m}$ ) |  |  |  |
| :--- | ---: | ---: | ---: |
| $\mathrm{M}_{1}$ | $2 / 0.25$ | $\mathrm{M}_{6}$ | $24 / 0.25$ |
| $\mathrm{M}_{2}$ | $2 / 0.25$ | $\mathrm{M}_{7}$ | $3 / 0.25$ |
| $\mathrm{M}_{3}$ | $2 / 0.25$ | $\mathrm{M}_{\mathrm{c}}$ | $\mathrm{W} / 0.25$ |
| $\mathrm{M}_{4}$ | $2 / 0.25$ |  |  |
| $\mathrm{M}_{5}$ | $0.5 / 0.25$ |  |  |

Fig. P14
15. Fig. P15 shows a comparator with OPAMP and offset cancellation. In this circuit, when switch $Q_{3}$ turns off, charge injection causes two extra errors to OPAMP input $\mathrm{V}^{\prime \prime}$ due to channel charge and clock feedthrough. The former can be attributed to the charge in transistor channel, which flows out from the channel region to the drain and source junctions. The latter is due to the overlap capacitance $\left(\mathrm{C}_{\mathrm{ov}}\right)$ of transistor between the gate and the junctions. Assume $\mathrm{V}_{\mathrm{DD}}=1.8 \mathrm{~V}$ and $\mathrm{V}_{\mathrm{tn}}=0.5 \mathrm{~V}$.
(a) Derive the OPAMP input voltage change $\left(\Delta \mathrm{V}^{\prime \prime}\right)$ due to channel charge and clock feedthrough in terms of $\mathrm{V}_{\mathrm{DD}}, G N D, \mathrm{~V}_{\mathrm{tn}}, \mathrm{C}_{\mathrm{ox}}, \mathrm{W}, \mathrm{L}, \mathrm{L}_{\mathrm{ov}}, \mathrm{C}$. (Hint: $\mathrm{C}_{\mathrm{ov}}=\mathrm{C}_{\mathrm{ox}} \times \mathrm{W} \times \mathrm{L}_{\mathrm{ov}}$, where $\mathrm{L}_{\mathrm{ov}}$ is the overlap length between gate and the junctions)
(b) Let $\mathrm{C}=3 \mathrm{pF}, \mathrm{C}_{\mathrm{ox}}=5 \mathrm{fF} /(\mu \mathrm{m})^{2},(\mathrm{~W} / \mathrm{L})_{1 \sim 3}=10 \mu \mathrm{~m} / 0.5 \mu \mathrm{~m}, \mathrm{~L}_{\mathrm{ov}}=0.2 \mu \mathrm{~m}$. Calculate the voltage change due to channel charge and clock feedthrough and total voltage change.

16. A single-stage fully differential OPAMP and its common-mode feedback (CMFB) circuit are shown in

Fig. P16, where $\mathrm{V}_{\mathrm{BN}}$ and $\mathrm{V}_{\mathrm{CM}}$ are DC voltage and the transistor sizes are given in Table P16. Assume $\mu_{\mathrm{n}} \mathrm{Cox}_{\mathrm{ox}}=100 \mu \mathrm{~A} / \mathrm{V}^{2}, \mu_{\mathrm{p}} \mathrm{Cox}_{\mathrm{ox}}=40 \mu \mathrm{~A} / \mathrm{V}^{2}, \mathrm{~V}_{\mathrm{tn}}=-\mathrm{V}_{\mathrm{tp}}=0.5 \mathrm{~V}, \mathrm{~V}_{\mathrm{DD}}=1.8 \mathrm{~V}, \lambda \mathrm{n}=\lambda \mathrm{p}=0.05 / \mathrm{L}(\mu \mathrm{m}), \mathrm{I}_{\mathrm{D}} \mathrm{M} 1=\mathrm{I}_{\mathrm{D}} \mathrm{M} 2=8 \mu \mathrm{~A}$ and body effect is negligible. (Neglect $\lambda$ and when determining DC voltage and current.)
(a) For proper CMFB operation, briefly explain which one of A and B should be connected to $\mathrm{v}_{\text {CTRL }}$ ?
(b) Calculate the DC gain of the common-mode loop gain.
(Hint: common-mode loop gain $=\frac{\mathrm{v}_{\mathrm{ctr}}(\mathrm{s})}{\mathrm{v}_{\mathrm{oc}}(\mathrm{s})} \cdot \frac{\mathrm{v}_{\mathrm{o}}{ }^{+}(\mathrm{s})}{\mathrm{v}_{\mathrm{ctrI}}(\mathrm{s})}$ or $\left.\frac{\mathrm{v}_{\mathrm{ctr}}(\mathrm{s})}{\mathrm{v}_{\mathrm{oc}}(\mathrm{s})} \cdot \frac{\mathrm{v}_{\mathrm{o}}{ }^{-}(\mathrm{s})}{\mathrm{v}_{\mathrm{crtr}}(\mathrm{s})}\right)$


Fig. P16
17. For the circuit shown in Fig. P17, assuming $\mu_{\mathrm{n}} \mathrm{Cox}_{\mathrm{o}}=100 \mu \mathrm{~A} / \mathrm{V}^{2}, \mu_{\mathrm{p}} \mathrm{Cox}_{\mathrm{ox}}=30 \mu \mathrm{~A} / \mathrm{V}^{2}, \mathrm{~V}_{\mathrm{tn}}=-\mathrm{V}_{\mathrm{tp}}=0.6 \mathrm{~V}$, $\mathrm{V}_{\mathrm{DD}}=1.8 \mathrm{~V}, \lambda_{\mathrm{n}}=\lambda_{\mathrm{p}}=0.05 / \mathrm{L}(\mu \mathrm{m}), \alpha=2$.
(a) If devices are perfectly matched, calculate $\mathrm{V}_{\mathrm{O}}$ and I
(b) If $(\mathrm{W} / \mathrm{L})_{2}$ becomes $3.1 / 0.25$ and $(\mathrm{W} / \mathrm{L})_{4}$ becomes $9.9 / 0.25$, calculate $\mathrm{V}_{\mathrm{O}}$.


Fig. P17
18. A fully-differential folded-cascode OPAMP is shown in Fig.P18(a), where it's input bias voltage is 0.9 V . Assume that $\mathrm{V}_{\mathrm{ov}}=0.2 \mathrm{~V}$ for all MOSFET except $\mathrm{M}_{9} \& \mathrm{M}_{10}$ and body effect can be neglected, and $\mathrm{V}_{\mathrm{DD}}=1.8 \mathrm{~V}, \mu_{\mathrm{n}} \mathrm{C}_{\mathrm{ox}}=200 \mu \mathrm{~A} / \mathrm{V}^{2}, \mu_{\mathrm{p}} \mathrm{Cox}_{\mathrm{ox}}=80 \mu \mathrm{~A} / \mathrm{V}^{2}, \mathrm{~V}_{\mathrm{tn}}=-\mathrm{V}_{\mathrm{tp}}=0.4 \mathrm{~V}, \lambda=\lambda_{\mathrm{n}}=-\lambda_{\mathrm{p}}=0.2 / \mathrm{L}(\mu \mathrm{m})$.
(a) Derive the output resistance ( $\mathrm{R}_{\mathrm{out}}$ ) with parameter of MOSFET. ( $\mathrm{g}_{\mathrm{mx}}$ and $\mathrm{r}_{\mathrm{dsx}}$ for $\mathrm{M}_{\mathrm{x}}$ )
(b) Calculate the DC gain and maximum negative slew rate, all the size of MOSFET are list in Table P18.

Assume that the total output capacitance is 2 pF at both $\mathrm{V}_{\text {out }+} \& \mathrm{~V}_{\text {out-. }}$
(c) Fig.P18(b) shows a common-mode feedback circuit, derive $\mathrm{V}_{\text {ctrl }}$ when output common-mode voltage is stable. (Parameters you can use: $\mathrm{V}_{\text {out }}, \mathrm{V}_{\text {out }}, \mathrm{V}_{\mathrm{CM}}, \mathrm{V}_{\mathrm{B} 4}, \mathrm{C}_{\mathrm{s}}$ and $\mathrm{C}_{\mathrm{c}}$. Hint: charge conservation)
(d) If $\mathrm{V}_{\mathrm{CM}}=0.9 \mathrm{~V}, \mathrm{C}_{\mathrm{c}}=\mathrm{C}_{\mathrm{s}}$ and output common-mode voltage is stable, determine the voltage of $\mathrm{V}_{\mathrm{B} 4}$.


Table P18
Transistor dimension (in $\mu \mathrm{m}$ )

| (in $\mu \mathrm{m})$ |  |  |  |
| :--- | ---: | :--- | :--- |
| $\mathrm{M}_{1}$ | $5 / 0.5$ | $\mathrm{M}_{6}$ | $29 / 0.5$ |
| $\mathrm{M}_{2}$ | $5 / 0.5$ | $\mathrm{M}_{7}$ | $12 / 0.5$ |
| $\mathrm{M}_{3}$ | $50 / 0.5$ | $\mathrm{M}_{8}$ | $12 / 0.5$ |
| $\mathrm{M}_{4}$ | $50 / 0.5$ | $\mathrm{M}_{9}$ | $15 / 0.5$ |
| $\mathrm{M}_{5}$ | $29 / 0.5$ | $\mathrm{M}_{10}$ | $15 / 0.5$ |

Fig. P18(a)


Fig. P18(b)
19. Derive the input-referred offset voltage of the circuit in Fig. P19. (Neglect channel length modulation and body effect.) Show the result in terms of $\Delta(\mathrm{W} / \mathrm{L})_{\mathrm{N}}, \Delta(\mathrm{W} / \mathrm{L})_{\mathrm{P}}, \mathrm{V}_{\mathrm{t} 1 \sim 4},(\mathrm{~W} / \mathrm{L})_{\mathrm{N}},(\mathrm{W} / \mathrm{L})_{\mathrm{P}}, \mathrm{I}_{\mathrm{N}}, \mathrm{I}_{\mathrm{P}}, \mathrm{V}_{\text {ovN }}$, and $\left|\mathrm{V}_{\text {OVP }}\right|$, where $\mathrm{V}_{\mathrm{t} 1 \sim 4}$ are the threshold voltages of $\mathrm{M}_{1 \sim 4}$.

$$
\left\{\begin{array}{l}
\Delta(\mathrm{W} / \mathrm{L})_{\mathrm{N}}=(\mathrm{W} / \mathrm{L})_{1}-(\mathrm{W} / \mathrm{L})_{2}, \Delta(\mathrm{~W} / \mathrm{L})_{\mathrm{P}}=(\mathrm{W} / \mathrm{L})_{3}-(\mathrm{W} / \mathrm{L})_{4} \\
(\mathrm{~W} / \mathrm{L})_{\mathrm{N}}=\frac{(\mathrm{W} / \mathrm{L})_{1}+(\mathrm{W} / \mathrm{L})_{2}}{2},(\mathrm{~W} / \mathrm{L})_{\mathrm{P}}=\frac{(\mathrm{W} / \mathrm{L})_{3}+(\mathrm{W} / \mathrm{L})_{4}}{2} \\
\mathrm{I}_{\mathrm{N}}=\frac{\mathrm{I}_{1}+\mathrm{I}_{2}}{2}, \mathrm{I}_{\mathrm{P}}=\frac{\mathrm{I}_{3}+\mathrm{I}_{4}}{2} \\
\mathrm{~V}_{\mathrm{OVN}}=\sqrt{\frac{2 \mathrm{I}_{\mathrm{N}}}{\mathrm{k}_{\mathrm{n}}^{\prime}(\mathrm{W} / \mathrm{L})_{\mathrm{N}}}},\left|\mathrm{~V}_{\mathrm{OVP}}\right|=\sqrt{\frac{2\left|\mathrm{I}_{\mathrm{P}}\right|}{\mathrm{k}_{\mathrm{p}}^{\prime}(\mathrm{W} / \mathrm{L})_{\mathrm{P}}}}
\end{array}\right.
$$

(Hint: For $\varepsilon \ll 1, \sqrt{1+\varepsilon} \approx 1+\varepsilon / 2$ and $(\sqrt{1+\varepsilon})^{-1} \approx 1-\varepsilon / 2$.)

20. A non-overlapped clock circuit and its input $v_{\text {IN }}$ are shown in Fig. P20(a) and Fig. P20(b). Assume the gate delays of NOR gate and inverter are $\mathrm{t}_{\mathrm{dN}}$ and $\mathrm{t}_{\mathrm{dI}}$, respectively. The $v_{\mathrm{IN}}$ period $T \gg \mathrm{t}_{\mathrm{dN}}, \mathrm{t}_{\mathrm{dI}}$.
(a) Please draw the waveform including all state transitions triggered by the falling edge of $v_{\text {IN }}$ for each of $v_{\mathrm{IN}}$ ', $\Phi_{1}, \Phi_{2}, \Phi_{3}$ and $\Phi_{4}$ and specify each edge delay relative to $v_{\mathrm{IN}}$ in terms of $\mathrm{t}_{\mathrm{dN}}$ and $\mathrm{t}_{\mathrm{dI}}$.
(b) Fig. P20(d) shows a comparator using an OPAMP, where the switch control signal is shown in Fig. P20(c) and the OPAMP is assumed to be ideal.
(1) According to the pulses of $\Phi_{1}, \Phi_{2}$, and $\Phi_{3}$, please derive the time-domain $v_{\text {out }}(\mathrm{nT})$ in $v_{\mathrm{n}}(\mathrm{nT})$, $v_{\mathrm{n}}(\mathrm{nT}-\mathrm{T} / 2)$ and $v_{\mathrm{in}}(\mathrm{nT})$ when the OPAMP noise $\left(v_{\mathrm{n}}\right)$ is considered.
(2) Assume the OAPMP gain A is $1000 \mathrm{~V} / \mathrm{V}$ (virtual short can be created at input nodes) where the noise $\left(v_{n}\right)$ is white with the value of $3.2(\mu \mathrm{~V} / \sqrt{\mathrm{Hz}})$ and the sampling frequency is 2 MHz . Please find the noise power in a bandwidth of 0 to 20 kHz using noise shaping function of correlated double sampling. (Hint: $z=\mathrm{e}^{\mathrm{j} \omega \mathrm{T}}$ )


Fig. P20(c)


Fig. P20(d)


$$
\rightarrow t
$$

21. For the fully-differential folded-cascode OPAMP shown in Fig. P21(a), the transistor sizes are given in Table P21. Assume $\mu_{\mathrm{n}} \mathrm{Cox}_{\mathrm{ox}}=90 \mu \mathrm{~A} / \mathrm{V}^{2}, \mu_{\mathrm{p}} \mathrm{Cox}=30 \mu \mathrm{~A} / \mathrm{V}^{2}, \mathrm{~V}_{\mathrm{tn}}=-\mathrm{V}_{\mathrm{tp}}=0.7 \mathrm{~V}, \mathrm{~V}_{\mathrm{DD}}=1.8 \mathrm{~V}, \mathrm{I}_{\mathrm{D} 2}=3 \times \mathrm{I}_{\mathrm{D} 6}=90 \mu \mathrm{~A}$, $\mathrm{C}_{\mathrm{L}}=4.5 \mathrm{pF}$, and junction capacitances and body effect can be ignored.
(a) Design a bias circuit for generating the required bias voltages.
(b) Calculate the power consumption of the OPAMP, the unity-gain frequency, phase margin, and slew rate excluding the common-mode feedback (CMFB) circuit.
(c) Estimate the frequency of the second pole caused by parasitic capacitances at the drains of M1 and M2 using $\mathrm{C}_{\mathrm{gs}(\text { (verlap) }-\mathrm{i}}, \mathrm{C}_{\mathrm{gd}(\text { (overlap) }-\mathrm{i}}$ and $\mathrm{C}_{\mathrm{ox}}$. (Hint: Assume $\mathrm{C}_{\mathrm{gs}-\mathrm{i}}=2 / 3 * \mathrm{WLC}_{\mathrm{ox}}+\mathrm{W}^{*} \mathrm{C}_{\mathrm{gs}(\text { (overlap)-i. }}$.)
(d) Briefly explain operational principle of the CMFB circuit shown in Fig. P21(b)?
(e) Why CMFB circuit is required in fully-differential amplifier circuit? (10\%)
(f) From Fig. P21(c), assume $g_{m, 12}=g_{m, 13}=g_{m, 14}=g_{m, 15}$, please calculate the common-mode loop gain in term of $\mathrm{r}_{\mathrm{d}, \mathrm{i}}$ and $\mathrm{g}_{\mathrm{m}, \mathrm{i}}$. (Hint: common-mode loop gain $=\frac{v_{\text {cntrl }}}{v_{\text {cm }}} \cdot \frac{v_{\text {out }}}{v_{\text {cntrl }}}$ )
(g) Could nodes from $\mathrm{V}_{\mathrm{B} 2}$ to $\mathrm{V}_{\mathrm{B} 5}$ be connected with the control voltage, $\mathrm{V}_{\text {cntrl }}$, of a general CMFB circuit, which doesn't specifically refer to the CMFB circuit shown in Fig. P21(b), for achieving common-mode voltage control as well? Give explanations on your answer. (10\%)
(h) Assume thermal noise power of the input transistor M1 is $\mathrm{V}_{\mathrm{n}}{ }^{2}$. Calculate the total input-referred thermal noise power excluding the CMFB and bias circuits. (15\%)

Table P21


Fig. P21(a)


Fig. P21(b)


Fig. P21(c)

